Radioactivity and Half-Life

All elements with more than 82 protons have unstable nuclei (i.e. Bi and beyond!) and are said to be radioactive. This is because there are too many protons in too small a volume to be stable – the repulsive forces among the protons are too strong to allow such nuclei to exist. There are, however, certainly isotopes of elements smaller than 82 that are also unstable. Scientists view nuclear instability not only in terms of nuclear size but also due to nuclear binding energy and the ratio of neutrons to protons.
Nuclear Binding Energy

For the nucleus to remain intact, the nucleons must be bound together by attractive forces strong enough to overcome the repulsive force between protons. This binding energy is defined as the energy released when a nucleus is formed from its component nucleons. Physicists have discovered that the mass of a nucleus is less than the sum of its component nucleons (protons and neutrons). The mass that is “lost” is known as mass defect. This mass is converted to energy used to “bind” the nucleons together – binding energy. If the binding energies of the nuclei of naturally occurring isotopes are calculated, it is found that atoms with the lowest and highest mass numbers have the smallest binding energies per nuclear particle. Elements having intermediate mass numbers have the greatest binding energy per nuclear particle.
The elements with the greatest binding energy per nucleon have the most stable nuclei. The greater the binding energy, the more difficult it is to pull the nucleus apart. Therefore, it follows that nuclei of elements with the smallest and largest mass numbers are less stable than nuclei of elements with intermediate mass numbers.

Any nuclear reaction involving an isotope with high binding energy per nucleon is difficult to start because of the large amount of energy required to break the nucleus apart, and it is difficult to perpetuate because of the small return on the energy invested.
Neutron to Proton Ratio

One theory of nuclear structure assumes that nucleons exist in energy levels within the nucleus. In accord with this theory, it can be shown that the most stable nuclei, and hence nuclei in which nucleons occupy the lowest energy level, are those with certain neutron-proton combinations. This becomes apparent when the number of neutrons is plotted versus the number of protons for the known stable isotopes.
Several facts can be derived from analysis of the plot of the number of neutrons versus the number of protons.

1. Stable nuclei are confined to a narrow zone indicating that the neutron-to-proton ratio (n/p) required for stability is relatively restricted.

2. The n/p ratio of stable nuclei increases with an increase in the number of protons. The stable isotopes of elements 1 to 20 have a n/p ratio of 1 or greater, while stable isotopes of elements 21 to 82 have n/p ratios greater than 1. Thus, the greater the number of protons in a nucleus, the greater the number of neutrons per proton required to form a stable nucleus.

3. Elements with more than 83 protons can form no stable nuclei. Thus, no stable nucleus with more than 83 protons can form regardless of the number of neutrons. It appears that nuclear forces cannot permanently exceed repulsive forces when more than 83 protons are assembled.
Radioactive elements become stable by emitting particle radiation and high energy electromagnetic radiation. These occur as three basic types and they were discovered when a radioactive source (such as U-238) was placed in a lead container with a small opening. The radiation coming out of the opening was subjected to an electric field and it was shown that the radiation consisted of three types:
• Particles deflected toward the negative plate – called alpha (α) particles
• Particles deflected toward the positive plate – called beta (β) particles
• Electromagnetic waves unaffected by the plates – called gamma (γ) waves
Types of Radiation

I. Alpha Decay

- Involves emission of a 2 proton-2 neutron unit from the nucleus; this unit is a helium nucleus
- Symbol is \(^4\text{He} (\alpha)\)
- Slow speed
- Poor penetrating power (can be stopped by sheet of paper)
- High ionizing capacity (when hitting an atom it can “knock off” an atom’s valence electron causing it to become an ion)

or break a molecule into positive and negative radicals
Example: $^{226}_{88}\text{Ra} \rightarrow ^{4}_{2}\text{He} + ^{222}_{86}\text{Rn}$

note the mass number (P + N) decreases by 4 and the atomic number (P only) decreases by 2
Beta Decay

- Involves emission of a high speed electron from the nucleus
- A neutron breaks down to a proton (which remains in the nucleus) and an electron which is ejected from the nucleus
- fairly high speed
- Moderate penetrating power (can be stopped by the thickness of your chemistry textbook
- Moderate ionizing capacity
- Symbol is $^o_e (\beta)$
Example: $^{214}_{82}\text{Pb} \rightarrow ^{0}_{-1}\beta + ^{214}_{83}\text{Bi}$

Note the atomic number increases by 1 while the mass number stays the same.
I. Gamma Radiation

- Travel at speed of light
- High penetrating power
- Very small ionizing capacity
- Emissions of gamma rays reduce the energy content of a nucleus without change in atomic or mass number
- Symbol is $\gamma$
Note the decay series of the isotope U-238 to the stable Pb-206 isotope. U-238 has a half-life of about $4.5 \times 10^9$ years (approximately the age of the earth). The ratio of U-238 to Pb-206 in a sample rock is used in geologic dating. The diagram below illustrates the decay series of uranium-238.
IV. Positron production

- Particle with same mass as an electron but opposite charge
- Has the effect of changing a proton to a neutron
- Results no change in mass number but a decrease of 1 in atomic number
- Symbol is $^0_+e$

Example: $^{22}_{11}\text{Na} \rightarrow ^0_+e + ^{22}_{10}\text{Ne}$
V. Electron Capture

- An inner-orbital electron is captured by the nucleus
- Does not occur often and is accompanied by gamma radiation

Example: \[ ^{201}_{80}\text{Hg} + ^0_{-1}\text{e} \rightarrow ^{201}_{79}\text{Au} + ^0_{\lambda}\text{e} \]
The Regents reference table (Table O) below shows the notation and symbols used in nuclear chemistry. You should become very familiar with the notation and symbols.

<table>
<thead>
<tr>
<th>Name</th>
<th>Notation</th>
<th>Symbol</th>
</tr>
</thead>
<tbody>
<tr>
<td>alpha particle</td>
<td>$^{4}\text{He}$ or $^{6}\alpha$</td>
<td>$\alpha$</td>
</tr>
<tr>
<td>beta particle (electron)</td>
<td>$^{0}<em>{-1}\text{e}$ or $^{0}</em>{-1}\beta$</td>
<td>$\beta^-$</td>
</tr>
<tr>
<td>gamma radiation</td>
<td>$^{0}_{0}\gamma$</td>
<td>$\gamma$</td>
</tr>
<tr>
<td>neutron</td>
<td>$^{1}_{0}\text{n}$</td>
<td>$n$</td>
</tr>
<tr>
<td>proton</td>
<td>$^{1}<em>{1}\text{H}$ or $^{1}</em>{1}\text{p}$</td>
<td>$p$</td>
</tr>
<tr>
<td>positron</td>
<td>$^{0}<em>{+1}\text{e}$ or $^{0}</em>{+1}\beta$</td>
<td>$\beta^+$</td>
</tr>
</tbody>
</table>
Nuclear Decay Reactions

1. Write balanced nuclear equations for the following processes:

a) the decay of gold-198:
\[ ^{198}_{79}\text{Au} \rightarrow ^{0}_{-1}\text{e} + ^{198}_{80}\text{Hg} \]

b) the decay of uranium-235:
\[ ^{235}_{92}\text{U} \rightarrow ^{4}_{2}\text{He} + ^{231}_{90}\text{Th} \]

c) the decay of phosphorous-32:
\[ ^{32}_{15}\text{P} \rightarrow ^{0}_{-1}\text{e} + ^{32}_{16}\text{S} \]

d) the decay of potassium-37:
\[ ^{37}_{19}\text{K} \rightarrow ^{0}_{+1}\text{e} + ^{37}_{18}\text{Ar} \]

e) the decay of francium-220
\[ ^{220}_{87}\text{Fr} \rightarrow ^{4}_{2}\text{He} + ^{216}_{85}\text{At} \]
2. A radioisotopes half-life is 1.000 minutes.

a) Given that the initial mass of a sample of this radioisotope is 12.00 g, calculate the mass of the radioisotope *that has not decayed* after 1.00 min, 2.00 min, 3.00 min, 4.00 min, 5.00 min, and 6.00 min.

b) Use the information you have just calculated to draw a graph of mass of radioisotope remaining vs time.
a) By interpolation of this graph, estimate the grams of radioisotope left after 1.5 min.

b) By interpolation, estimate the amount of time that must elapse in order for 1.0 g of the radioisotope to be present.

\[ \approx 3.6 \text{ min} \]
2. The initial mass of a sample of a certain radioisotope is 100.0 g. After 1.0 hour, 80.0 g of it remains; after 2.0 hours, 64.0 g remains; after 4.0 hours, 41.0 g remains; and after 6.0 hours, 26.2 g remains.

a) On the grid below, use this information to draw a graph of mass of radioisotope remaining vs time.

b) Use the graph to estimate the half-life of the radioisotope. (Hint: find the x-value at which half of the initial mass of the radioisotope remains.)

\[ \text{~3 hrs} \]

b) Use your answer to b to calculate the amount of time for 25 g of the radioisotope to remain.

\[ 100 \rightarrow 50 \rightarrow 25 \rightarrow \text{two half-lives} \rightarrow 2 \times 3 = 6 \text{ hrs} \]

c) By extrapolation of the graph, find the mass of radioisotope remaining after 8.0 hours.

\[ \sim 19 \text{ g} \]
Half-Life

The half-life of an unstable isotope is the time required for one-half of the nuclei in a sample to decay:

\[ X \text{ g} \rightarrow \frac{1}{2}X \text{ g} \rightarrow \frac{1}{4}X \text{ g} \rightarrow \frac{1}{8}X \text{ g} \rightarrow \frac{1}{16}X \text{ g} \rightarrow \text{ etc} \]

The half-life of a radioactive isotope is independent of temperature and pressure and the mass of the unstable element. The half-life is also characteristic of that particular isotope. The Regents reference table (Table N) lists the half-life and decay mode for selected nuclides.

Half-life problems can be solved using the above concept. You may set up a table with the following headings that may make the problem easier:

<table>
<thead>
<tr>
<th>Mass</th>
<th>half-life number</th>
<th>time</th>
<th>fraction</th>
</tr>
</thead>
</table>

Radiocarbon Dating

One of the best known radioactive isotopes is carbon-14. The half-life of carbon-14 is 5730 years. This radioactive isotope is produced in the Earth’s atmosphere by the action of cosmic rays on ordinary atmospheric nitrogen (N-14). (Cosmic rays are streams of high-energy charged particles and neutrons from outer space that collide with atoms in the Earth’s upper atmosphere.) This action results in the nitrogen-14 being converted to carbon-14. The reaction is as follows:

\[
\frac{14}{7}\text{N} + \frac{1}{0}\text{n} \rightarrow \frac{14}{6}\text{C} + \frac{1}{1}\text{H}
\]

New atoms of C-14 are produced at the same rate that the isotope decays. Scientists assume that the production of C-14 has been essentially constant for a long time. After being produced by the cosmic rays, the C-14 is then oxidized in the atmosphere to form $^{14}\text{CO}_2$, which mixes with the $^{12}\text{CO}_2$ already present in the atmosphere. As a result, the atmosphere always contains a fixed ratio of $^{14}\text{CO}_2$ to $^{12}\text{CO}_2$.

What makes C-14 such an important isotope? The answer is in the way in which carbon dioxide is used by plants and animals. Carbon dioxide is an essential part of the process of photosynthesis in plants. Photosynthesis is the process by which green plants use the sun’s energy to convert carbon dioxide and water into sugars and starches. The sugars and starches, in turn, are food for animals that eat the plants and exhale carbon dioxide. Because this cycle exposes plants and animals to a constant source of C-14, the amount of this isotope in living plants and animals is constant. The emission of beta particles is likewise constant as the isotope decays.

The incorporation of C-14 into plant and animal tissues stops once the organism dies. The emission of beta particles will then drop as the C-14 decays. After 5730 years the rate of beta emissions will have dropped to one half the rate in living organisms; after 11,460 years the rate will have dropped to one quarter, and so forth. By determining the rate of beta emission from plant and animal remains or products – such as wooden objects, textiles, and leather – scientists can estimate the age of these objects. Such estimates are accurate up to about 7000 years and give a reasonable approximation up to 30,000 years. (After this length of time, the rate of beta emissions is too slow to be measured reliably.)
### Table N

**Selected Radioisotopes**

<table>
<thead>
<tr>
<th>Nuclide</th>
<th>Half-Life</th>
<th>Decay Mode</th>
<th>Nuclide Name</th>
</tr>
</thead>
<tbody>
<tr>
<td>$^{198}_{\text{Au}}$</td>
<td>2.69 d</td>
<td>$\beta^-$</td>
<td>gold-198</td>
</tr>
<tr>
<td>$^{14}_{\text{C}}$</td>
<td>5730 y</td>
<td>$\beta^-$</td>
<td>carbon-14</td>
</tr>
<tr>
<td>$^{37}_{\text{Ca}}$</td>
<td>175 ms</td>
<td>$\beta^+$</td>
<td>calcium-37</td>
</tr>
<tr>
<td>$^{60}_{\text{Co}}$</td>
<td>5.26 y</td>
<td>$\beta^-$</td>
<td>cobalt-60</td>
</tr>
<tr>
<td>$^{137}_{\text{Cs}}$</td>
<td>30.23 y</td>
<td>$\beta^-$</td>
<td>cesium-137</td>
</tr>
<tr>
<td>$^{53}_{\text{Fe}}$</td>
<td>8.51 min</td>
<td>$\beta^+$</td>
<td>iron-53</td>
</tr>
<tr>
<td>$^{220}_{\text{Fr}}$</td>
<td>27.5 s</td>
<td>$\alpha$</td>
<td>francium-220</td>
</tr>
<tr>
<td>$^{3}_{\text{H}}$</td>
<td>12.26 y</td>
<td>$\beta^-$</td>
<td>hydrogen-3</td>
</tr>
<tr>
<td>$^{131}_{\text{I}}$</td>
<td>8.07 d</td>
<td>$\beta^-$</td>
<td>iodine-131</td>
</tr>
<tr>
<td>$^{37}_{\text{K}}$</td>
<td>1.23 s</td>
<td>$\beta^+$</td>
<td>potassium-37</td>
</tr>
<tr>
<td>$^{42}_{\text{K}}$</td>
<td>12.4 h</td>
<td>$\beta^-$</td>
<td>potassium-42</td>
</tr>
<tr>
<td>$^{85}_{\text{Kr}}$</td>
<td>10.76 y</td>
<td>$\beta^-$</td>
<td>krypton-85</td>
</tr>
<tr>
<td>$^{16}_{\text{N}}$</td>
<td>7.2 s</td>
<td>$\beta^-$</td>
<td>nitrogen-16</td>
</tr>
<tr>
<td>$^{19}_{\text{Ne}}$</td>
<td>17.2 s</td>
<td>$\beta^+$</td>
<td>neon-19</td>
</tr>
<tr>
<td>$^{32}_{\text{P}}$</td>
<td>14.3 d</td>
<td>$\beta^-$</td>
<td>phosphorus-32</td>
</tr>
<tr>
<td>$^{239}_{\text{Pu}}$</td>
<td>$2.44 \times 10^4$ y</td>
<td>$\alpha$</td>
<td>plutonium-239</td>
</tr>
<tr>
<td>$^{226}_{\text{Ra}}$</td>
<td>1600 y</td>
<td>$\alpha$</td>
<td>radium-226</td>
</tr>
<tr>
<td>$^{222}_{\text{Rn}}$</td>
<td>3.83 d</td>
<td>$\alpha$</td>
<td>radon-222</td>
</tr>
<tr>
<td>$^{90}_{\text{Sr}}$</td>
<td>28.1 y</td>
<td>$\beta^-$</td>
<td>strontium-90</td>
</tr>
<tr>
<td>$^{99}_{\text{Tc}}$</td>
<td>$2.13 \times 10^5$ y</td>
<td>$\beta^-$</td>
<td>technetium-99</td>
</tr>
<tr>
<td>$^{212}_{\text{Th}}$</td>
<td>$1.4 \times 10^{10}$ y</td>
<td>$\alpha$</td>
<td>thorium-232</td>
</tr>
<tr>
<td>$^{233}_{\text{U}}$</td>
<td>$1.62 \times 10^5$ y</td>
<td>$\alpha$</td>
<td>uranium-233</td>
</tr>
<tr>
<td>$^{235}_{\text{U}}$</td>
<td>$7.1 \times 10^5$ y</td>
<td>$\alpha$</td>
<td>uranium-235</td>
</tr>
<tr>
<td>$^{238}_{\text{U}}$</td>
<td>$4.51 \times 10^9$ y</td>
<td>$\alpha$</td>
<td>uranium-238</td>
</tr>
</tbody>
</table>

*ms = milliseconds; s = seconds; min = minutes; h = hours; d = days; y = years*
Problem 1

A radioactive element has a half-life of 4 hours. What fraction of an original sample will remain at the end of 12 hours?

\[
\frac{12 \text{ hr}}{4 \text{ hr}} = 3 \text{ half-lives}
\]

\[
\frac{1}{2} \rightarrow \frac{1}{4} \rightarrow \frac{1}{8}
\]

Problem 2

A sample of Sr-90 has a mass of 1.0 gram after 116.4 years. Calculate the mass of the original sample.

\[
\frac{116.4 \text{ yr}}{28.1 \text{ yr}} = 4 \text{ half-lives}
\]

\[
1 \text{ g} \rightarrow 2 \text{ g} \rightarrow 4 \text{ g} \rightarrow 8 \text{ g} \rightarrow 16 \text{ g}
\]
Problem 3

Exactly 1.0 g of Na-24 decomposes by beta emission to 1/8 g in 45 hours. Determine its half-life.

\[ \text{Half-Life} = \frac{\text{time}}{\# \text{ half-lives}} = \frac{45 \text{ hours}}{3 \text{ half-lives}} = 15 \text{ hours/half-life} \]

Problem 4

If the initial mass of a sample of cesium-137 is 1.00 kg, calculate the mass that will remain after 151 years.

\[ \text{H-L} = 30.23 \text{ yrs} \]

151 yrs. \[ \frac{\text{151 yrs.}}{30.23 \text{ yrs}} = 5 \text{ half-lives} \]

\[ 1000 \text{ g} \rightarrow \frac{500}{2} \rightarrow \frac{250}{2} \rightarrow 125 \rightarrow 62.5 \]

\[ \text{Final mass} = 31.3 \text{ g} \]
Problem 5

A sample of fossilized wood that, when alive, would have contained 24 g of carbon-14. It now contains 1.5 g of carbon-14. Determine the approximate age of the sample.

\[ \begin{array}{c}
24 \text{g} \rightarrow 12 \text{g} \rightarrow 6 \text{g} \rightarrow 3 \text{g} \rightarrow 1.5 \text{g} \\
4 \text{H-L} \times \frac{5730 \text{yr}}{1 \text{H-L}} = 22,920 \text{ys}
\end{array} \]

Problem 6

A 64 g sample of germanium-66 is left undisturbed for 12.5 hours. At the end of that period, only 2.0 g remain. Calculate the half-life of this material.

\[ \begin{array}{c}
64 \text{g} \rightarrow 32 \text{g} \rightarrow 16 \text{g} \rightarrow 8 \text{g} \rightarrow 4 \text{g} \rightarrow 2 \text{g} \\
\therefore \frac{12.5 \text{hr}}{5 \text{H-L}} = 2.5 \text{hr/H-L}
\end{array} \]
Problem 7

Cobalt-60 has a half-life of 5.26 years. If a pellet that has been in storage for 26.5 years contains 14.5 g of cobalt-60, determine the mass of this isotope that was present when the pellet was put into storage.

\[
H-L = 5.26 \text{ yrs}
\]

\[
\frac{26.5 \text{ yr}}{5 \text{ H-L}} = 5 \text{ H-L}
\]

\[
14.5 \text{ g} \quad \xrightarrow{5} \quad 2.9 \text{ g} \quad \xrightarrow{4} \quad 0.58 \text{ g} \quad \xrightarrow{3} \quad 0.116 \text{ g} \quad \xrightarrow{2} \quad 0.023 \text{ g} \quad \xrightarrow{1} \quad 0.0046 \text{ g}
\]
Review Questions

1. A radioactive atom will lose the greatest amount of mass when it emits

   (1) a neutron  (2) a proton  (3) a beta particle  (4) an alpha particle

2. According to the equation $X \rightarrow ^{208}_{82}\text{Pb} + ^{4}_{2}\text{He}$, the nucleus correctly represented by $X$ is

   $^82_{2}$

   (1) $^{204}_{82}\text{Hg}$  (2) $^{212}_{84}\text{Po}$  (3) $^{204}_{80}\text{Bi}$  (4) $^{212}_{84}\text{Pb}$

3. In the equation $^{226}_{88}\text{Ra} \rightarrow ^{222}_{86}\text{Rn} + X$, $X$ represents

   (1) a neutron  (2) a proton  (3) a beta particle  (4) an alpha particle

4. In the reaction $^{24}_{11}\text{Na} \rightarrow ^{24}_{11}\text{Mg} + X$, the particle represented by letter $X$ is

   (1) a proton  (2) a neutron  (3) an electron  (4) a positron

5. When $^{234}_{90}\text{Th}$ emits a beta particle, the element formed is

   (1) $^{234}_{90}\text{Ra}$  (2) $^{234}_{90}\text{Th}$  (3) $^{234}_{91}\text{Pa}$  (4) $^{234}_{92}\text{U}$
6. A radioactive element has a half-life of 4 hours. How much of the original radioactive material will remain at the end of 12 hours?

(1) 1/8  (2) 1/4  (3) 1/3  (4) 1/2

7. As the pressure on a gaseous radioisotope increases, its half-life

(1) decreases  (2) increases  (3) remains the same

8. A 40.0 milligram sample of $^{33}$P decays to 10.0 milligrams in 50.0 days. What is the half-life of $^{33}$P?

(1) 12.5 days  (2) 25 days  (3) 37.5 days  (4) 75.0 days

9. What total mass of a 16 gram sample of $^{60}$Co will remain unchanged after 15.9 years?

(1) 1.0 g  (2) 2.0 g  (3) 8.0 g  (4) 4.0 g

10. The half-life of $^{14}$C is 5,730 years. What fraction of a 1.0 gram sample of $^{14}$C would remain after 17,190 years?

(1) 1/2  (2) 1/4  (3) 1/8  (4) 1/16
Nuclear Reactions

It was discovered that the mass of an atomic nucleus is less than the sum of the masses of individual protons and neutrons making up the nucleus. The mass which is lost is known as mass defect and the energy equivalent is known as the binding energy of the nucleus. Recall iron has the highest binding energy per nucleon.

I. Transmutations – conversion of one element to a different one.

   a) natural – alpha and beta decay

   b) artificial – involves “hitting” a nucleus with an alpha particle or bare proton in a particle accelerator. Particle accelerators use magnetic fields to accelerate charged particles (like protons, electrons and alpha particles but not neutrons) to near the speed of light before colliding them.

Example: \[ ^{14}_7 \text{N} + ^{4}_2 \text{He} \rightarrow ^{17}_8 \text{O} + ^{1}_1 \text{H} \]

Note: the transuranic elements (those beyond uranium) are all man-made:

Example: \[ ^{238}_{92} \text{U} + ^{1}_0 \text{n} \rightarrow ^{239}_{92} \text{U} \rightarrow ^{239}_{93} \text{Np} + ^{0}_{-1} \text{e} \rightarrow ^{239}_{94} \text{Pu} + ^{0}_{-1} \text{e} \]
I. Nuclear Fission

- splitting a large nucleus into smaller nuclei of similar size with release of energy
- there are two fissionable isotopes: U-235 and Pu-239

example: $^{235}_{92} \text{U} + ^1_0 \text{n} \rightarrow ^{139}_{56} \text{Ba} + ^{94}_{36} \text{Kr} + 3 ^1_0 \text{n} + \text{ENERGY}$
two factors of monumental consequence:

- the difference in mass between reactants and products indicated a significant mass lost – this mass was converted to energy via $E = mc^2$
- the potential for a **chain reaction** – a reaction that is self-sustaining – that is, the reaction generates the means to trigger additional reactions. The amount of fissionable material that will support a chain reaction is termed the **critical mass**.

Uncontrolled fission reaction = atomic bomb
Controlled fission reaction = nuclear power plants
A chain reaction

fission fragment

neutron

U-235

fission fragment
http://www.ucsusa.org/sites/default/files/images/2015/08/np-how-Pressurized-Water-Reactors-work.gif
Nuclear Fission Reactor

Diagram of a nuclear fission reactor with labeled components:
- Concrete confinement shell
- Steam generator
- Steel containment vessel
- Control rod drive
- Control rods
- Fuel rods
- Coolant and moderator (heavy water or liquid sodium)
- Circulating coolant
- Pump
Main components:

**Nuclear Fuel** – Uranium-235 is the only naturally occurring isotope of uranium that will undergo fission. The percentage of U-235 in a pure sample of uranium is only 0.7% and this amount is insufficient to sustain a chain reaction. The U-235 is separated from pure uranium to produce “enriched” uranium (about 3% U-235). This mixture is used to produce uranium oxide for use as fuel in the reactor. Pellets of uranium oxide are packed in stainless steel tubes called **fuel rods**.

**Moderators** – used to slow down the neutrons produced as a result of fission reactions. The moderator functions to absorb some of the energy of the high kinetic energy neutrons to slow them down so they can be captured by the U-235 nuclei. Some common materials used for moderators include graphite, molten sodium, and heavy water (water containing a deuterium hydrogen).

**Control Rods** – function to control the rate of the fission reaction by absorbing neutrons. Substances such as cadmium or boron are very effective absorbers of neutrons. Control rods made from one of these substances are located side-by-side with the fuel rods in the reactor. By inserting and withdrawing these rods, the supply of neutrons can be regulated and, in cases of emergency, shut off completely.

**Coolants** – the primary coolant, which is often water at high pressure, is circulated around the reactor core where it absorbs the tremendous amount of heat generated by the fission reaction. Since the water is under pressure it reaches 300°C without boiling and is pumped into a steam generator. The steam generator contains water under normal pressure. The heat from the primary coolant is transferred to this water (secondary coolant) which causes it to form steam. The steam is then used to drive a turbine which generates electricity. The primary coolant, now at a lower temperature, is pumped back into the reactor core and the cycle continues.

**Shields** – the core of a reactor is surrounded by a containment vessel in which the primary coolant circulates. The walls of this vessel are lined with thick steel slabs to reduce the flow of radiation from the core. The containment vessel, in turn, is surrounded by thick concrete blocks designed to protect personnel from radiation exposure.
Advantages: provides much needed energy

Disadvantages: radioactive waste
thermal pollution of river water
possibility of mechanical/human error

Breeder Reactor – some control rods are replaced with rods containing U-238. The U-238 absorb neutrons and then decay to form fissionable Pu-239.
More nuclear equation writing:

(a) Plutonium-230 can be produced by bombarding uranium-238 with alpha particles. How many neutrons will be produced as a byproduct of each reaction?

\[
\begin{align*}
\text{Pu} & \rightarrow \text{Pu} + 2^1n \\
239_{92}U + 4^2He & \rightarrow 230_{94}Pu + 1^0n \\
238_{92}U + 2^1H & \rightarrow 238_{93}Np + 2^1n
\end{align*}
\]

(b) Another method for producing plutonium-239 is by bombarding uranium-238 with deuterium (hydrogen-2), which produces neptunium-238 and 2 neutrons. The unstable neptunium then decays to form plutonium-238. Write the nuclear equations for this two-step reaction. What other particle is produced in the second reaction?

\[
\begin{align*}
\text{Pu} & \rightarrow \text{Pu} + 1^0e \\
238_{92}U + 2^1H & \rightarrow 238_{93}Np + 2^1n \\
238_{93}Np & \rightarrow 239_{94}Pu + 1^0e
\end{align*}
\]

(c) When bombarded with neutrons, lithium-6 produces an alpha particle and an isotope of hydrogen. Write the nuclear equation for this reaction and identify the isotope of hydrogen produced.

\[
\begin{align*}
\text{Li} & \rightarrow \text{He} + \text{H} \\
6_{3}Li + 1^0n & \rightarrow 4^2He + 1^1H
\end{align*}
\]

(d) With what particle would you bombard sulfur-32 to produce hydrogen-1 and phosphorous-32? Write the appropriate nuclear equation.

\[
\begin{align*}
\text{S} & \rightarrow \text{P} + \text{H} \\
32_{16}S + 1^0n & \rightarrow 32_{15}P + 1^1H
\end{align*}
\]
Nuclear Waste

When the fuel rods in fission reactors become “spent”, they contain a mixture of highly radioactive isotopes. These include both the fission products and what remains of the nuclear fuel. Some of these fission products have very short half-lives (on the order of seconds) while others have half-lives of hundreds of thousands of years. All nuclear power plants currently store their spent fuel rods in holding tanks containing water. The water cools the rods and acts as a radiation shield. The spent fuel rods are held in these water “pools” for many years as they continue to generate heat.

In 1982 the U.S. Congress passed the Nuclear Waste Policy Act, which established a timetable for choosing and preparing sites for deep underground disposal of radioactive materials. The disposal plan calls for the incorporation of the spent nuclear fuel into blocks of borosilicate glass that will be packed in corrosion-resistant metal containers and then buried in deep, stable rock formations. In 1987 Congress amended the Nuclear Waste Policy Act to make Yucca Mountain in Nevada the primary potential site.
Nuclear Waste Locations in the US

77 Locations

- These sites store spent nuclear fuel, high-level radioactive waste, and/or surplus plutonium destined for geologic disposal.

- As of now, Yucca Mountain does not store any nuclear waste.
I. Nuclear Fusion

- Two small nuclei (hydrogen) collide to form a bigger nucleus (He) and release energy.
- Significant mass loss converted to energy.
- No chain reaction; no critical mass.
- Fusion reactions are the source of the Sun’s energy; millions of tons of matter (H) are converted to energy in the Sun every second.
- In order for fusion reactions to occur, exceedingly high temperatures are needed (to overcome repulsive forces between protons); it is necessary to “confine” the plasma with electromagnets.
- Fusion bomb = uncontrolled fusion = hydrogen bomb.

Example: 

\[
\begin{align*}
\text{(fusion reaction)} & : \quad ^3_1H + ^2_1H \rightarrow ^4_2\text{He} + ^1_1\text{n} + \text{ENERGY} \\
\text{Advantages of nuclear fusion:} & \\
\text{• clean} & \\
\text{• Few radioactive products} & \\
\text{• Fuel inexhaustible (H in water in oceans)} & \\
\text{• No possibility of reaction going out of control} & 
\end{align*}
\]
Radioisotopes

Uses include as tracers (C-14), dating (C-14 and U-238/Pb-206 ratio), diagnosis of brain tumors (Tc) thyroid disease (I-131), etc.
Detecting Radiation

X-rays and radiation emitted by radioisotopes are called ionizing radiation. Recall ionizing radiation is radiation with enough energy to knock electrons off some atoms they strike to produce ions. You cannot detect ionizing radiation with any of your senses. Instead, various instruments and monitoring devices are used for this purpose. One such device, called a Geiger counter, uses a gas-filled metal tube to detect radiation. The figure below shows the construction of a Geiger counter. The tube has a central wire electrode that is connected to a power supply. When ionizing radiation penetrates a thin window at one end off the tube, the gas inside the tube becomes ionized. Because of the ions and free electrons produced, the gas becomes an electrical conductor. Each time a Geiger tube is exposed to radiation, current flows. The bursts of current drive electronic counters or cause audible clicks from a built-in speaker. Geiger counters are used primarily to detect beta radiation.
Smoke detectors contain a radioactive isotope. The radioactive emissions of the smoke detector ionize air to conduct a current is sensed by the detector. When smoke interrupts current flow to the detector, an alarm sounds.
Review Questions

1. There are no known stable isotopes of the element with atomic number
   (1) 20   (2) 38   (3) 56   (4) 88

2. Given the equation: \( ^{238}_{92}U + ^4_{2}He \rightarrow ^{241}_{94}Pu + ^1_{0}n \)
   The reaction is an example of  (1) addition   (2) condensation   (3) substitution   (4) transmutation

3. Which of the following nuclei would have the greatest binding energy per nucleon?
   (1) hydrogen   (2) helium   (3) iron   (4) uranium

4. Particles are given sufficient energy to enter into a nuclear reaction by
   (1) heating   (2) placing in an accelerator   (3) use of a catalyst   (4) grinding to increase surface area

5. Which of the following particles cannot be speeded up in a particle accelerator?
   (1) proton   (2) deuteron   (3) neutron   (4) alpha particle
6. In the equation $^1_2\text{H} + ^1_1\text{H} \rightarrow ^4_2\text{He} + X$, the term X represents

(1) a neutron  (2) a positron  (3) an electron  (4) an alpha particle

7. According to the equation $X \rightarrow ^{208}_{82}\text{Pb} + ^4_2\text{He}$, X represents the nucleus

(1) $^{204}_{80}\text{Hg}$  (2) $^{212}_{84}\text{Po}$  (3) $^{204}_{80}\text{Bi}$  (4) $^{212}_{84}\text{Pb}$

8. The energy equivalent of the mass defect is known as

(1) an alpha particle  (2) binding energy  (3) half-life  (4) kinetic energy

9. The equation $^1_1\text{H} + ^1_1\text{H} \rightarrow ^4_2\text{He}$ represents

(1) fusion  (2) fission  (3) alpha decay  (4) k-capture

10. When neutrons and protons combine to form a stable nucleus, the actual mass of the nucleus, compared to the total mass of its parts, is

(1) less  (2) greater  (3) the same
11. The decay of uranium to lead is an example of

(1) natural radioactivity  (2) artificial transmutation  (3) fission  (4) fusion

12. Which of the following nuclei is naturally radioactive?

(1) H-2  (2) F-19  (3) Fe-56  (4) U-238

13. Which substance is used as a moderator in a nuclear reactor?

(1) aluminum  (2) graphite  (3) plutonium  (4) helium

14. A requirement for a fusion reactor is

(1) extremely high temperatures  (2) heavy atomic nuclei as fuel  (3) inexpensive equipment  (4) operators with little training

15. The ratio of carbon-14 in a test sample to that in the atmosphere is used to determine the

(1) pressure of the atmosphere  (2) pollution in the atmosphere  (3) age of the sample  (4) chemical composition of the sample
16. In a fission reaction, which of the following is needed to continue the chain reaction?

(1) protons  (2) neutrons  (3) electrons  (4) deuterium

17. Which of the following could be used as a fuel in a nuclear fission reactor?

(1) U-235  (2) U-238  (3) protium  (4) deuterium

18. A sample of wood was analyzed and found to have only one-half the ratio of C-14 to C-12 as in a living sample. The half-life of C-14 = 5700 years. The wood is probably about

(1) 2800 years old  (2) 5700 years old  (3) 11,200 years old  (4) 17,000 years old

19. The amount of Pb-206 in a sample of a rock which contains uranium

(1) will increase with time  (2) will decrease with time  (3) will not change with time

20. In a nuclear reactor the amount of uranium present remains fairly constant. The rate of the reaction is controlled by the amount of

(1) barium  (2) alpha particles  (3) beta particles  (4) neutrons
21. A substance which can be used as both a moderator and the coolant in a nuclear reactor is
(1) graphite (2) cadmium (3) liquid sodium (4) plutonium

22. A reactor in which more fuel is produced is called a
(1) fusion reactor (2) breeder reactor (3) steam reactor (4) reversible reactor

23. The fuel produced in a breeder reactor is
(1) uranium (2) plutonium (3) cadmium (4) helium

24. One of the difficulties of producing a fusion reactor is the
(1) high temperatures needed to begin the reaction (2) lack of a suitable fuel (3) high radioactivity of the products (4) lack of a suitable catalyst

25. When radioisotopes are used in the medical treatment or diagnosis and are ingested by the patient, it is important that they
(1) be inexpensive (2) have long half-lives (3) have short half-lives (4) emit only alpha radiation

26. Which of the following radioisotopes is used in the diagnosis of the diseases of the thyroid?
(1) I-131 (2) co-60 (3) Tc-99 (4) U-235

27. In a nuclear reactor, the neutrons can be slowed by collisions with
(1) uranium atoms (2) graphite (3) cadmium (4) boron